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## Electric Circuits



**Unit: 6 | Lecture: 27**  
**Capacitors and Inductors:**  
**Series and Parallel Capacitors**

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## Capacitors and Inductors

- 6.1 Introduction
- 6.2 Capacitors
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- 6.5 Series and Parallel Inductors



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## 6.3 Series and **Parallel** Capacitors

To obtain the equivalent capacitor  $C_{eq}$  of  $N$  capacitors in parallel,

Note that the capacitors have the same voltage  $v$  across them.

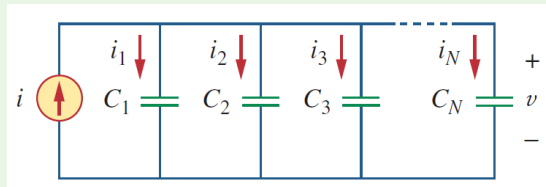
Applying KCL

$$i = i_1 + i_2 + i_3 + \dots + i_N$$

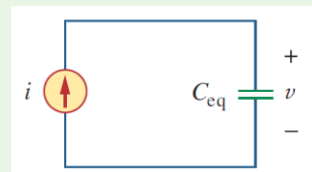
$$i = C_1 \frac{dv}{dt} + C_2 \frac{dv}{dt} + C_3 \frac{dv}{dt} + \dots + C_N \frac{dv}{dt} = C_{eq} \frac{dv}{dt}$$

$$C_{eq} = C_1 + C_2 + C_3 + \dots + C_N$$

The equivalent capacitance of  $N$  parallel-connected capacitors is the sum of the individual capacitances.



Parallel-connected  $N$  capacitors



equivalent circuit

## 6.3 Series and **Parallel** Capacitors

To obtain the equivalent capacitor  $C_{eq}$  of  $N$  capacitors in series,

Note that the same current  $i$  flows through the capacitors.

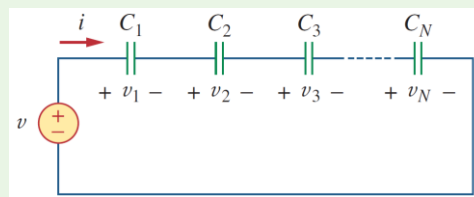
Applying KVL

$$v = v_1 + v_2 + v_3 + \dots + v_N$$

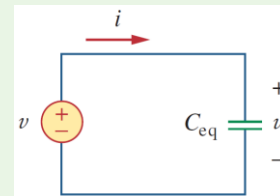
$$\therefore v_k = \frac{1}{C_k} \int_{t_0}^t i(\tau) d\tau + v_k(t_0)$$

$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} + \dots + \frac{1}{C_N}$$

The equivalent capacitance of series capacitors is the reciprocal of the sum of the reciprocals of the individual capacitances.



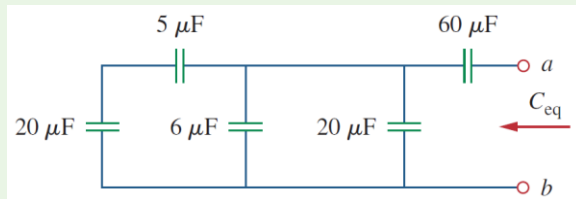
Series-connected  $N$  capacitors



equivalent circuit

## Example 6.6

Find the equivalent capacitance seen between terminals  $a$  and  $b$



The  $20\ \mu\text{F}$  and  $5\ \mu\text{F}$  capacitors are in **series**;

$$\frac{20 \times 5}{20 + 5} = 4\ \mu\text{F}$$

This  $4\ \mu\text{F}$  capacitor is in **parallel** with the  $6\ \mu\text{F}$  and  $20\ \mu\text{F}$  capacitors;

$$4 + 6 + 20 = 30\ \mu\text{F}$$

This  $30\ \mu\text{F}$  capacitor is in **series** with the  $60\ \mu\text{F}$  capacitor;

$$C_{\text{eq}} = \frac{30 \times 60}{30 + 60} = 20\ \mu\text{F}$$

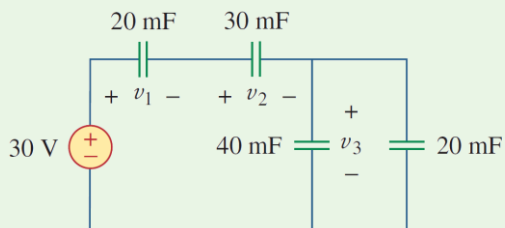
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## Example 6.7 (1)

Find the voltage across each capacitor.

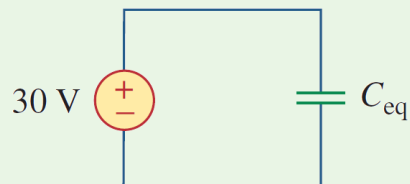


The two capacitors  $40$  and  $20\ \text{mF}$  are in **parallel**

$$40 + 20 = 60\ \text{mF}$$

This  $60\text{-mF}$  capacitor is in **series** with the  $20\text{-mF}$  and  $30\text{-mF}$  capacitors.

$$C_{\text{eq}} = \frac{1}{\frac{1}{60} + \frac{1}{30} + \frac{1}{20}}\ \text{mF} = 10\ \text{mF}$$



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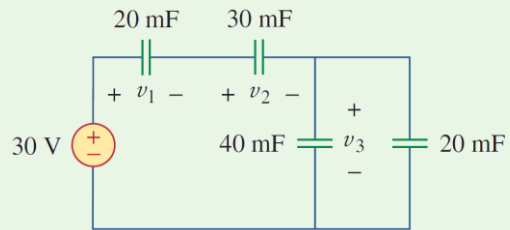
(6)

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## Example 6.7 (2)

The total charge is

$$q = C_{\text{eq}}v = 10 \times 10^{-3} \times 30 = 0.3 \text{ C}$$



This is the charge on the 20-mF and 30-mF capacitors, because they are in series with the 30-V source.

$$v_1 = \frac{q}{C_1} = \frac{0.3}{20 \times 10^{-3}} = 15 \text{ V}$$

$$v_2 = \frac{q}{C_2} = \frac{0.3}{30 \times 10^{-3}} = 10 \text{ V}$$

use KVL to determine

$$v_3 = 30 - v_1 - v_2 = 5 \text{ V}$$

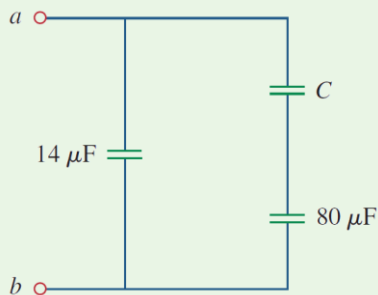
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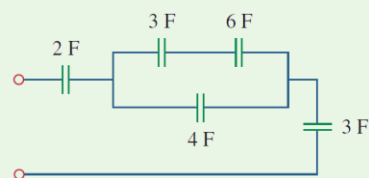
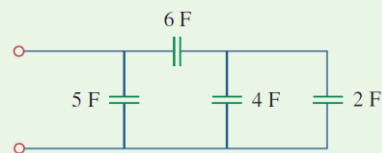
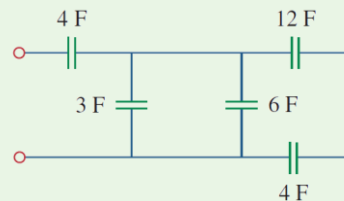
## Problems to Solve by yourself

(1) Series-connected 20-pF and 60-pF capacitors are placed in parallel with series-connected 30-pF and 70-pF capacitors. Determine the equivalent capacitance.

(2) The equivalent capacitance at terminals *a-b* in the circuit is 30  $\mu\text{F}$ . Calculate the value of *C*.



(3) Determine the equivalent capacitance for each of the circuits.



(8)

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